

**e8 = Norm[bb] + Norm[cc]**

 $4\sqrt{5} + \sqrt{86}$ 

**e9 = FullSimplify[e7 ⩵ e8] False**

7. | a.c |, | a || c |

**e10 = Norm[aa.cc]**

**24**

```
e11 = Norm[aa] Norm[cc]
```
 $\sqrt{3010}$ 

9.  $15a.b + 15a.c$ ,  $15a.(b+c)$ 

**e12 = 15 aa.bb + 15 aa.cc**

**300**

```
e13 = 15 aa.(bb + cc)
```
**300**

## **17 - 20 Work**

Find the work done by a force **p** acting on a body if the body is displaced along the straight segment *AB* from *A* to *B*. Sketch *AB* and **p**.

17. p = {2, 5, 0}, A: {1, 3, 3}, B: {3, 5, 5}

```
ClearAll["Global`*"]
aA = {1, 3, 3}; bB = {3, 5, 5}
{3, 5, 5}
pP = {2, 5, 0}
{2, 5, 0}
dis = bB - aA
{2, 2, 2}
```

```
wW = dis.pP
  14
\texttt{cosinealpha} = \texttt{N} \left[ \begin{array}{c} \texttt{wW} \ \texttt{m} \end{array} \right]Norm[dis] Norm[pP]
                                                              1
0.750479
alpha = ArcCos[cosinealpha]
0.72201
```
Mathematica doesn't like to use degrees, but one way to get there is

**1. Degree 57.2958 % alpha 41.3681**

The above way of calculating the work moves everything into the frame of reference of the origin. However, the problem description requested a view of *AB*, so that is drawn in red.



Note: drawing arcs in Mathematica's 3D plot is not very easy. I found several recommended methods on line, but finally just flogged an approximated arc out of Blender.

19. p = {0, 4, 3}, A: {4, 5, -1}, B: (1, 3, 0}

**ClearAll["Global`\*"]**

**pP = {0, 4, 3}; aA = {4, 5, -1}; bB = {1, 3, 0} {1, 3, 0}**

**dis = bB - aA {-3, -2, 1} wW = dis.pP -5**  $\texttt{cosinealpha} = \texttt{N} \left[ \begin{array}{c} \texttt{wW} \ \texttt{d} \end{array} \right]$ **Norm[dis] Norm[pP] -0.267261 alpha = ArcCos[cosinealpha] 1.84135 1. Degree 57.2958 % alpha 105.501**  $\,6\,$  $\overline{4}$  $\overline{2}$  $\mathbf 0$  ${0, 4, 3}$  $\overline{c}$ 105.5 degrees  $\{-3, -2, 1\}$  $\boldsymbol{z}$  $\mathbf 0$  $[0, 0, 0]$ 

1

The requested sketch is shown.

 $\overline{\mathbf{c}}$ 

**22 - 30 Angle between vectors** Let  $aA = \{1, 1, 0\}$ ;  $bB = \{3, 2, 1\}$ ;  $cC = \{1, 0, 2\}$ 

 $\overline{4}$ 

23. b, c

 $-2\frac{6}{4}$ 

 $-2$ 

 $\overline{0}$ 

 $\boldsymbol{x}$ 

**dotbc = bB.cC**

**5**

**e1 <sup>=</sup> dotbc Norm[bB] Norm[cC]**

$$
\sqrt{\frac{5}{14}} / N
$$
  
0.597614  
e2 = Arccos [e1]  
Arccos  $\left[\sqrt{\frac{5}{14}}\right] / N$   
0.930274  
e3 =  $\frac{e2}{\text{Degree}} / N$   
53.3008

**31 - 35 Orthogonality** is particularly important, mainly because of orthogonal coordinates, such as Cartesian coordinates, whose natural basis consists of three orthogonal unit vectors.

31. For what values of *a*1 are {*a*1, 4, 3} and {3, -2, 12} orthogonal?

```
ClearAll["Global`*"]
e1 = {a1, 4, 3}
```

```
{a1, 4, 3}
e2 = {3, -2, 12}
{3, -2, 12}
e3 = e1.e2
```

```
28 + 3a_1
```

```
Solve[e3 ⩵ 0]
```

$$
\left\{ \left\{ a_{1}\rightarrow-\frac{28}{3}\right\} \right\}
$$

33. Unit vectors. Find all unit vectors  $a = \{a_1, a_2\}$  in the plane orthogonal to  $\{4, 3\}$ 

```
ClearAll["Global`*"]
e1 = {4, 3}
{4, 3}
```
**e2 = Norm[e1] 5**  $e3 = \{a_1, a_2\}$ **{a1, a2} e4 = Norm[e3]**  $\sqrt{\text{Abs}[a_1]^2 + \text{Abs}[a_2]^2}$ **e5 = Solve[e1.e3 ⩵ 0 && Norm[e3] ⩵ 1]**  $\left\{\left\{a_1 \rightarrow \frac{3}{n}\right\}\right\}$ *a*  $\rightarrow$   $\rightarrow$   $\frac{4}{5}$ **}**,  $\{a_1 \rightarrow -\frac{3}{5}\}$ ,  $a_2 \rightarrow \frac{4}{5}$ 

**5**

## **36 - 40 Component in the direction of a vector**

Find the component of a in the direction of b. Make a sketch.

**5**

37.  $a = \{3, 4, 0\}, b = \{4, -3, 2\}$ 

## **ClearAll["Global`\*"]**

**5**

To find the component of **a** in the direction of **b**, I first need to find the angle separating them.

**5**  $\{\}$ 

```
e1 = {3, 4, 0}
{3, 4, 0}
e2 = {4, -3, 2}
{4, -3, 2}
e3 = e1.e2
    Norm[e1] Norm[e2]
0
e4 = ArcCos[e3]
π
2
```
These two vectors are perpendicular; therefore there is no projection  $(=0)$ .

```
e5 = Norm[e1] Cos[e4]
```
**0**



In a case like this, the component of b in a would normally be the projection of b onto a. Here however, the two vectors are perpendicular, so the projection (and the component), are zero. This graphic shows the arrowhead bug in Mathematica, talked about at *https://community.wolfram.com/groups/-/m/t/1302365* and *https://mathematica.stackexchange.com/questions/81306/arrowhead-becomes-unattached-to-line-in-a-graphics3d-manipulate?noredirect=1* and probably other places. In this case if the blue **tube** is not used, the arrowhead becomes detached and floats around outside the display cube.